#### 48th Lee Webb Math Field Day

California State University, Bakersfield Department of Mathematics

February 23, 2019

#### Junior Varsity Math Bowl

### Round 1

# Simplify

$$\frac{9}{1} + \frac{0}{2}$$

Two numbers are 9 apart and their sum is 31. What is the larger number?

What is the largest whole number that is less than 1000 and is a power of 2?

The squares of the lengths of the legs of a right triangle are 36 and 64. What is the length of the hypotenuse?

In the last election 3 out of every 7 voters were in favor of ballot measure Z. There were 35000 voters. What is the maximum number of "NO" votes possible?

The number corresponding to this year, 2019, can be factored as a product of two primes. What is the sum of the primes?

Simplify

 $2^{3^2}$ 

#### **Evaluate**

998 · 1002

The graph of a tenth degree polynomial can have at most how many "humps" (local maximum points)?

Alan bought 72 widgets. The first and last digits on the receipt are smudged, so we only know that the cost was \$\_957.9\_. What is leading digit of this number?

Alice, Harry, Chloe, and Sam all either always tells the truth or always lies. You hear the following:

Alice: "Alice and Chloe lie."

Harry: "Alice lies, and Sam is truthful."

Sam: "Alice lies."

Of the four people, how many are truth tellers?

#### Junior Varsity Math Bowl

### Round 2

With regard to the number 2019, what is the result if you divide the second largest digit by the second smallest digit?

A line segment is divided into two subsegments whose lengths have a ratio of 3:8. The total length of the segment is 253. What is the length of the shorter subsegment?

What is the sum of all possible values of *x* that satsify

$$(x+1)(x-5)=16$$
?

## Simplify

$$\frac{2}{5} \cdot \frac{3}{6} \cdot \frac{4}{7} \cdot \frac{5}{8} \cdot \frac{6}{9} \cdot \frac{7}{10}$$

How many different pairs of people can be chosen from a class of 25 students?

How many positive even numbers are less than 2000?

## Simplify:

$$2019^2 - 2018^2 + 2017^1 - 2016^1$$

A box manufacturer sells a rectangular box with volume 1000 cubic inches. Another one of their boxes has the width increased by 10 percent and the length decreased by 10 percent (and no change to the height). What is the volume of this second box?

## Suppose

$$(7^{3/2}8^{2/3}9^{1/4})^4 = 2^a 3^b 7^c$$

What is 
$$a + b + c$$
?

A right triangle is inscribed in a circle with radius 12.5. One of the legs has length 7. What is the length of the other leg?

This term, so far, Joshua has received a 90 on each of the 8 quizzes. What does he need to average on the last two quizzes to get a 95 over all average?

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### Round 3

What is half of a third of a fourth of 96?

Let C be a circle of area 18. In decimal form, to the nearest hundredth, what is the ratio of the circumference of C to the diameter of C?

What is the largest 3 digit number that is not a multiple of 3?

If  $\frac{20}{19}$  is written in decimal form, what is the first digit after the decimal point?

# Simplify

$$|(|4 - |8 - 11||) - 7|$$

A sock drawer has 5 red socks, 3 green socks, and 1 blue sock. Anne pulls out two socks. What is the probability that they are the same color?

Starting with the number 2019, a robot is asked to double a number and then square the result, and then triple the result, and then cube the result, and then divide by 2019 six times. What should the robot's answer be?

Calculate the sum of the numbers in the following array:

The angles in a regular polygon each measure 144 degrees. How many sides does the polygon have?

Let 
$$f(x) = x(x+1)(x+2)$$
. Evaluate 
$$\frac{f(5)f(7)}{f(4)f(6)}$$

The sides of a triangle have lengths 3, 4, and 5. If the side of length 5 is considered the base, then what is the altitude from that side?

#### Junior Varsity Math Bowl

# Round 4

Today is Feruary 23. What is the next number that ends with a 3 that is prime?

Today is Saturday, Feb. 23, 2019. Not counting today, how many days are left in 2019?

A triangle with a horizontal base has area 25. A line perpendicular to the altitude cuts through the triangle 1/5 of the way from the base to the apex. What is the area of the triangle that is above this line?

Suppose we have a sequence  $a_n$  with  $a_1=1$  and

$$a_n=\frac{n}{a_{n-1}}.$$

What is  $a_5$ ?

The first term of a geometric sequence is 5. The common ratio is  $2^{1/7}$ . The number 40 is in the sequence. What is index of the number 40? (I.e. where in the sequence is the number 40?)

Let [x] denote the greatest integer that is less than or equal to x. Simplify:

$$-\left([-\sqrt{1}] + [-\sqrt{2}] + [-\sqrt{3}] + [-\sqrt{4}]\right)$$

What is the sum of all the two-digit multiples of 9?

How many multiples of 7 are there that are greater than 700 and less than 800?

Solve for x:

$$2x^2 + 6 - x \cdot x = \frac{x^3}{x} + x$$

What is the distance between the points (2, 13, -3) and (8, 6, -9)

# Simplify:

$$\frac{1}{\frac{1}{1}+\frac{1}{2}+\frac{1}{3}+\frac{1}{4}}$$

#### Junior Varsity Math Bowl

18

See you this afternoon Varsity Math Bowl 2:15