52nd Lee Webb Math Field Day

California State University, Bakersfield Department of Mathematics

March 1, 2025

Junior Varsity Math Bowl

Round 1

Simplify

$$\frac{2}{2} \cdot \frac{0}{5}$$

A bowl has 35 green beans and red beans altogether. The number of green beans is 4 times the number of red beans. How many green beans are there?

This year number is a perfect square that ends with a 5. How many years from now, will this happen again?

A school has red, green, orange, and purple pens available for teachers to grade homework. At present, 46% of the pens are red, 15% are green, 12% are orange. What is the probability that a randomly chosen pen is purple?

When Sara flies her plane to Las Vegas, her plane averages 600 mph. On her way back, she averages 400 mph. What is Sara's average speed for the round trip?

What is the difference between the largest and the smallest prime factors of 52?

Rewrite 0.525252525252.... as fraction in lowest terms.

After shuffling, what is the probability that the top 3 cards are all aces? Answer as a fraction in lowest terms.

Suppose f(x) is a function that satisfies the functional equation

$$f(5x+5)=x-5$$

Evaluate f(2025).

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Round 2

What is the difference between the largest and smallest prime factors of 2025?

How many real solutions are there to

$$|x^2 + 2| + 3|x^2 + 1| \le 5$$
?

What is the 2025th term of the sequence that starts

 $1, 0, 3, 0, 2, 1, 0, 3, 0, 2, 1, 0, 3, 0, 2, 1, 0, \dots$

and continues with this pattern?

How many weeks are in a leap year? Answer as a "mixed number" - a whole number with a reduced fraction that is less than 1. E.g. $2\frac{3}{5}$

What is the measure, in degrees, of the complement of the supplement of a 115° angle?

2025 is a square. What is the smallest cube that is greater than 2025?

If one card is drawn randomly from a standard deck, what is the probability that it is a heart or an ace?

A circle is inscribed inside a square such that the area of the circle is 16π . What is the perimeter of the square?

What is the largest 2 digit number with exactly 4 factors, including itself?

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Round 3

In a standard deck, how many cards are not Kings, Queens, or Jacks?

Let C be a circle of radius $\frac{1}{2}\pi$. In decimal form, to the nearest hundredth, what is the value of the circumference of C divided by π ?

A standard deck is shuffled. What is the probability that the 10^{th} card is a 10?

The ratio of the measures of two complementary angles is 7:11. What is the measure, in degrees, of the larger angle?

In how many ways can a quarter be changed into dimes, nickels, and pennies?

Fifteen dogs have been entered into an ugly dog contest. First, Second, and Third Prizes will be awarded. In how many ways could the awards be presented?

(e.g. in how many ways could the first, second, and third place dogs be selected?)

Solve

$$20|x^2 - 5x + 6| + 25|x^2 - 4| = 0$$

Calculate the sum

$$\frac{25!}{24!} + \frac{24!}{23!} + \frac{23!}{22!} + \frac{22!}{21!} + \frac{21!}{20!}$$

The angles in a regular polygon each measure 179.5 degrees. How many sides does the polygon have?

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Round 4

Today is March 1. In "month day" format this is 31, which is a prime number. What is the "month day" for the first day last month whose "month day" is a prime?

A square is inscribed inside a circle with circumference 3π . What is the area of the square?

How many different combinations of one-dollar and 10-dollar notes are there such that the total value is \$2025?

Three lines intersect at points A, B, and C. Relative to triangle ABC, the exterior angle at A has measure 75° and the vertical angle opposite B has measure 45° . What is the degree measure of the triangle's vertex at C?

Jack has 8 dogs and he would like to take 3 of them for a walk. How many possible groups of 3 dogs could Jack choose?

Suppose that $5^{2z-1} = 125$. What is 5^z ?

Three students each took a test. Their median was 90 and their mean was 82. The range was 28. What are the three scores - list them in increasing order, separated by commas.

Suppose

$$2^{-x+2y}=4$$

and

$$9^{x-y} = 27$$

What is x?

If xyz = 2025 and x + y + z = 47, knowing that x, y, z are integers, what are the values of x, y, and z?

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See you this afternoon Varsity Math Bowl 2:15